

## KAUZMANN TEMPERATURE AND THE GLASS TRANSITION

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Kauzmann temperature was investigated on the  $\text{As}_2\text{Se}_3$  and  $\text{As}_2\text{S}_3$  bulk glasses. Novel StepScan DSC technique was used to separate processes during the glass transition on both reversible and irreversible parts. This method is necessary to obtain correct information especially when undercooled melt undergo glass transition and the exothermic change is masked by the increase of total heat flow. It was found that Kauzmann temperature of  $\text{As}_2\text{Se}_3$  bulk glass coincides with the low temperature onset in the glass transition range. Kauzmann temperature of  $\text{As}_2\text{S}_3$  was found markedly below the glass transformation range. From that follows that the glass transition of  $\text{As}_2\text{Se}_3$  can be considered as thermodynamic one, contrary to the glass transition of  $\text{As}_2\text{S}_3$ . From this point of view  $\text{As}_2\text{Se}_3$  is an ideal glass contrary to  $\text{As}_2\text{S}_3$  glass that preserves to a certain extent the undercooled melt nature.

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### 1. Introduction

In 1948 Kauzmann pointed out that the entropy of supercooled liquid decreases rapidly on cooling towards the kinetic glass transition temperature,  $T_g$ , and extrapolates to the entropy of the crystal not far below  $T_g$ , [1]. Temperature dependence of the entropy of glass intersects that of crystal at so called Kauzmann temperature,  $T_K$ . If the entropy of the supercooled liquid becomes lower than that of the stable crystal, it would eventually become negative at sufficiently low temperature, thereby violating the Third Law of Thermodynamics. This situation is named Kauzmann's paradox or entropy crisis, see e.g. [2-4] and references cited therein. The entropy crisis arises because the heat capacity of undercooled liquid is greater than that of crystal. Therefore, the entropy of fusion is consumed upon cooling and vanishes at Kauzmann temperature. One way of avoiding the entropy crisis is, for the liquid, to form an "ideal glass" at  $T_K$ . This is the thermodynamic view of the glass transition according to which the observable glass transition (for instance by viscosity or DSC measurements) is the manifestation of a second-order phase transition at Kauzmann temperature, masked by kinetics. According to Kauzmann, spontaneous freezing at kinetic glass transition prevents equilibration of supercooled liquid near  $T_K$ . Because kinetic glass transition is higher than Kauzmann temperature, it intervenes before the entropy crisis occurs. From it follows that the estimation of  $T_K$  can be obtained by extrapolation of supercooled liquid entropy below  $T_g$ , [2-4].

Novel experimental techniques of differential scanning calorimetry, temperature modulated DSC (TA Instruments) and, recently, StepScan DSC (Perkin-Elmer), have allowed to separate reversible thermodynamic processes from irreversible kinetic ones. It was found that the glass transition is represented by the reversible part, which is insensitive to the thermal history of glass. Hence the glass transition temperature depends only on the chemical composition [5-7]. Irreversible enthalpy change reflects the thermal history of a glass. Hence, the effect of both isothermal and non-

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isothermal aging proves at the moment of the glass transition measurement that the kinetic part superposed over the reversible (thermodynamic) one, [6,7]. It was also discovered that the irreversible enthalpy change in the course of the glass transition is associated with reversible change not only during the glass to supercooled liquid transformation (endothermic process) but also in the reverse direction (exothermic one), [6,7]. Stemming from these results the glass transition seems not to be only a kinetic phenomenon, as many authors believe, but it could be supposed that the glass transition is a reversible process in the thermodynamic sense [8,9].

From this perspective on the glass transition it is interesting to test whether Kauzmann temperature can be achieved and "ideal glass" in Kauzmann sense can exist in reality. The  $\text{As}_2\text{Se}_3$  and  $\text{As}_2\text{S}_3$  bulk glasses were chosen because of their easy preparation in high purity as well as possibility of slow cooling of its undercooled melt without crystallization. Nucleation temperature of  $\text{As}_2\text{Se}_3$  is lower than the crystallization one. On the other hand, crystalline  $\text{As}_2\text{Se}_3$  can be prepared relatively easily [10], contrary to crystalline  $\text{As}_2\text{S}_3$  [11].

## 2. Experimental

Bulk glasses of  $\text{As}_2\text{Se}_3$  and  $\text{As}_2\text{S}_3$  were prepared by direct synthesis from elements of 5N purity in evacuated silica ampoules in a rocking furnace (750 °C, 24 hrs.) and melts were quenched in air. Crystalline  $\text{As}_2\text{Se}_3$  was obtained by slow heating from the glass transition temperature up to 300 °C, followed by isothermal crystallization (24 hrs.) of undercooled melt at this temperature. Crystalline  $\text{As}_2\text{S}_3$  was obtained by our method described in [11] and checked by X-ray diffraction.

To obtain both temperature dependencies of  $C_p$  and irreversible enthalpy changes at the glass transition, Fig. 1a, as well as at the crystal melting (Fig. 1b), novel stepwise technique StepScan DSC and power compensated DSC Pyris 1 (both by Perkin-Elmer) were used. Crystalline samples were measured in the heating mode; cooling mode was used for measuring of non-crystalline material (undercooled melt and glass). Temperature step +1 or -1 °C and step heating rate +100 or -100 °C/min., followed by approx. 1 min. isothermal lag was used in all cases.

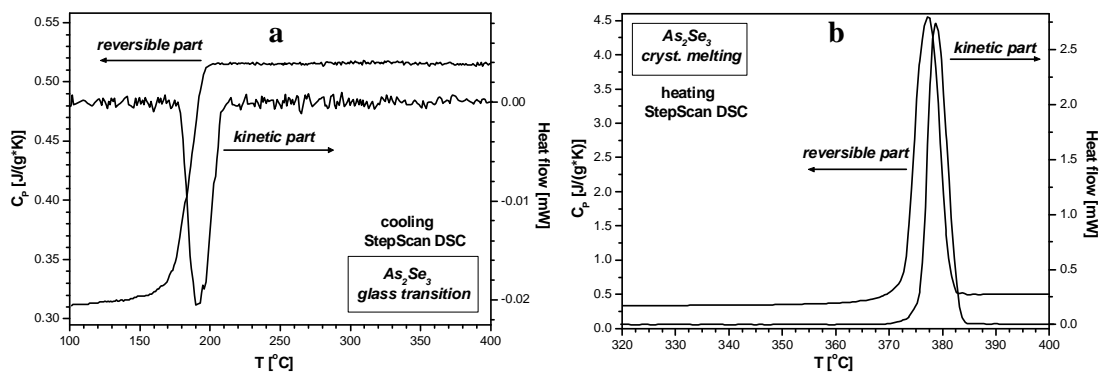


Fig. 1. StepScan DSC results,  $\text{As}_2\text{Se}_3$  system: a) glass transition during supercooled melt cooling, b) melting of crystals.

## 3. Results and discussion

Results obtained by StepScan DSC on the crystalline and glassy arsenic trichalcogenides have been used to calculate the temperature dependence of entropy changes (within experimental accuracy). The temperature dependence of the entropy change for both crystalline and non-crystalline samples is given by the sum of the thermodynamic contribution and of the enthalpy change of kinetic process divided by its temperature:

$$\Delta S(T) = \int_{T_1}^{T_2} \frac{C_p}{T} dT + \frac{\Delta H_{\text{kin}}}{T_x} \quad (1)$$

In this equation  $C_p$  is isobaric heat capacity,  $\Delta H_{\text{kin}}$  is enthalpy changes obtained from irreversible kinetic part,  $T_x$  is either the glass transition temperature,  $T_g$ , or the crystal melting one,  $T_m$ , and  $T_1 \ll T_g$  and  $T_2 \gg T_m$ .

In fact, because the irreversible kinetic processes are spread over indispensable temperature interval (see Fig. 1), the contribution of the kinetic part to the entropy change in course of the glass transformation and/or of the crystal melting was replaced by  $\Delta S_{\text{kin}}(T)$  and calculated according to equation:

$$\frac{\Delta H_{\text{kin}}}{T_x} \approx \Delta S_{\text{kin}}(T) = \frac{1}{m \cdot \beta} \int_{T_1}^{T_2} \frac{Q_{\text{kin}}(T)}{T} dT, \quad (2)$$

where  $m$  is the sample mass,  $\beta$  is the underlying heating/cooling rate,  $Q_{\text{kin}}(T)$  is the heat flow related to kinetic processes.

Using entropy-temperature dependence obtained, the Kauzmann temperature of  $\text{As}_2\text{Se}_3$  was found to be  $T_K = 164^\circ\text{C}$  (see Fig. 3). This temperature is  $23^\circ\text{C}$  below the glass transition temperature,  $T_g = 187^\circ\text{C}$ , [2].

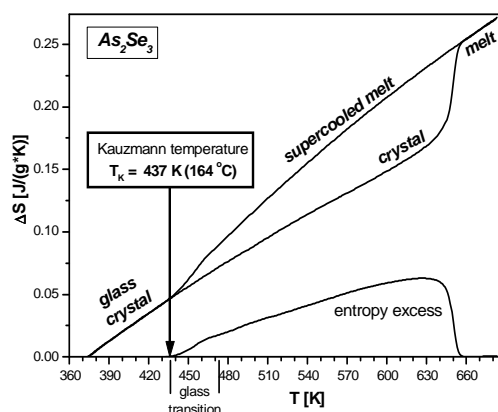


Fig. 2. Temperature dependence of both entropy of  $\text{As}_2\text{Se}_3$  system and entropy excess of supercooled melt and the Kauzmann temperature.

Confronting the obtained Kauzmann temperature and thermodynamic part of the glass transition of  $\text{As}_2\text{Se}_3$ , we have found that  $T_K$  is identifiable with the low- $T$  onset of the glass transition region (Fig. 4), and very close to the viscosity near the onset of  $T_g = 166^\circ\text{C}$  ( $\eta = 10^{12}$  Pa.s). The temperature of this low- $T$  onset is exactly that one at which supercooled liquid is completely transformed to glass. This result has physical meaning and according to the Kauzmann idea, the glass transition of  $\text{As}_2\text{Se}_3$  bulk glass is the thermodynamic one and this glass can be named an ideal glass.

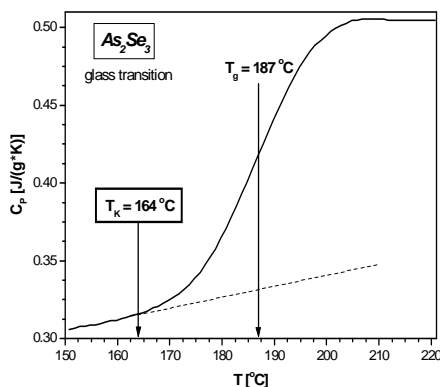


Fig. 3. Kauzmann temperature and the glass transition region (reversible part) of  $\text{As}_2\text{Se}_3$  bulk glass.

On the other hand, a surprising result was obtained on  $\text{As}_2\text{S}_3$  bulk glass. As one can find anywhere, this glass has been widely used as an "ideal glass" because of its easy preparation and extremely low crystallization tendency of its undercooled melt [12]. Kauzmann temperature of  $\text{As}_2\text{S}_3$  was found at around 97 °C (Fig. 4). This temperature is ~ 78 °C below low-T onset (175 °C) of the glass transition region and it is clear, that ideal glass transition (thermodynamic one) is masked by the kinetic effects at significantly higher temperature. Based on the idea of Kauzmann temperature, the  $\text{As}_2\text{S}_3$  glass contains some excess of the entropy of fusion and, therefore, glass preserves to a certain extent the undercooled melt nature.

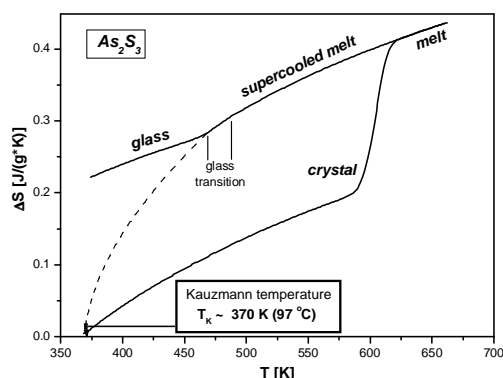


Fig. 4. Temperature dependence of entropy of  $\text{As}_2\text{S}_3$  system and approximation of the Kauzmann temperature.

Finally, we must point out that it is not possible to obtain the same results using conventional DSC because cooling scans over the glass transition region are distorted due to the simultaneous endothermic and exothermic events (for details see [6]).

#### 4. Conclusions

Using the StepScan DSC, we have shown, contrary to the commonly accepted opinion, that the undercooled liquid can really achieve the Kauzmann temperature and thus avoids the entropy crisis thermodynamically and not only by the kinetic effects. This ideal behavior was found for  $\text{As}_2\text{Se}_3$  undercooled melt, but, surprisingly, not for  $\text{As}_2\text{S}_3$  one.

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